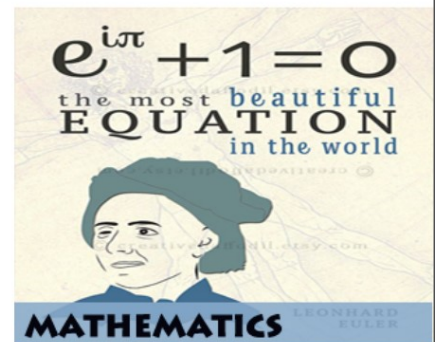
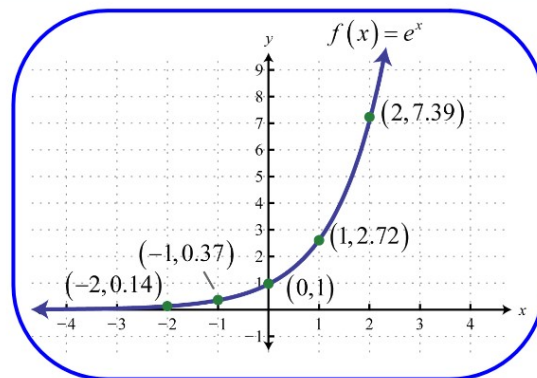


## The Base $e$

**Objectives** To explore the properties of functions of the form  $y = ab^x$   
To graph exponential functions that have base  $e$



Sometimes called "Euler's Number" after Swiss Mathematician Leonhard Euler,  $e$  is an irrational number that is approximately 2.718.

Even though  $e$  is an irrational number, it can be used as the base of an exponential function. The number  $e$  is sometimes called the natural base of an exponential function and is used extensively in scientific and other applications involving exponential growth and decay.

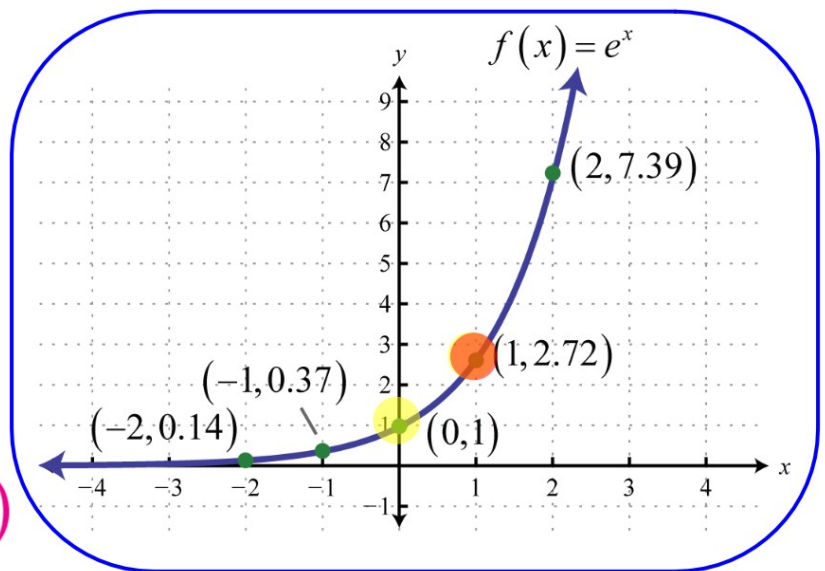
## The Base $e$

Domain:  $\{x \mid -\infty < x < \infty\}$ .

Range:  $\{y \mid y > 0\}$ .

The asymptote :  $y = 0$

The reference points :  $(0, 1)$ ,  $(1, e)$



$e$  is usually approximated to 2.72

## The Base $e$

### Graphing Combined Transformations of $f(x) = e^x$

When graphing combined transformations of  $f(x) = e^x$  that result in the function  $g(x) = a \cdot e^{x-h} + k$ , it helps to focus on two reference points on the graph of  $f(x)$ ,  $(0, 1)$  and  $(1, e)$ , as well as on the asymptote  $y = 0$ . The table shows these reference points and the asymptote  $y = 0$  for  $f(x) = e^x$  and the corresponding points and asymptote for the transformed function,  $g(x) = a \cdot e^{x-h} + k$ .

#### *Parent function*      *Transformation*

	$f(x) = e^x$	$g(x) = a \cdot e^{x-h} + k$
First reference point	$(0, 1)$	$(h, a + k)$
Second reference point	$(1, e)$	$(h + 1, ae + k)$
Asymptote	$y = 0$	$y = k$

## The Base $e$

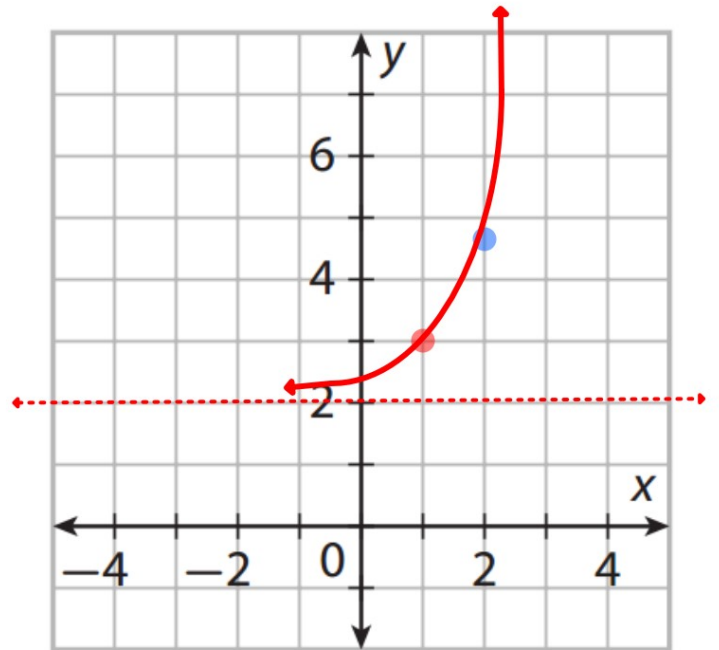
Graphing and Analyzing  $g(x) = e^{x-1} + 2$

*first reference point*

$$(h, a + k) \quad (1, 3)$$

$$(1 + h, ae + k) \quad (2, 2e + 2)$$

*second reference point*



## The Base $e$

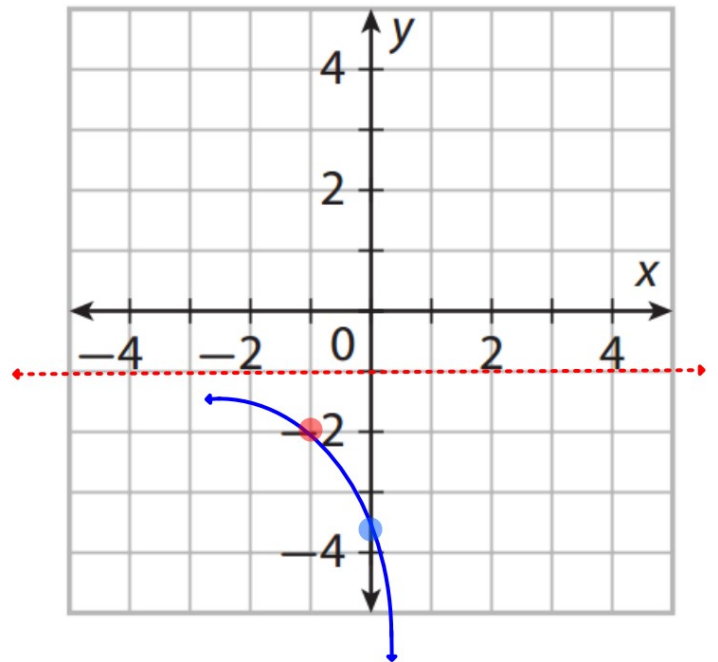
Graphing and Analyzing  $g(x) = -e^{x+1} - 1$

*first reference point*

$(h, a + k)$   $(-1, -2)$

$(1 + h, ae + k)$   $(0, -e - 1)$

*second reference point*



## The Base $e$

Writing Equations for Combined Transformations  
of  $f(x) = e^x$

$$g(x) = a \cdot e^{x-h} + k$$

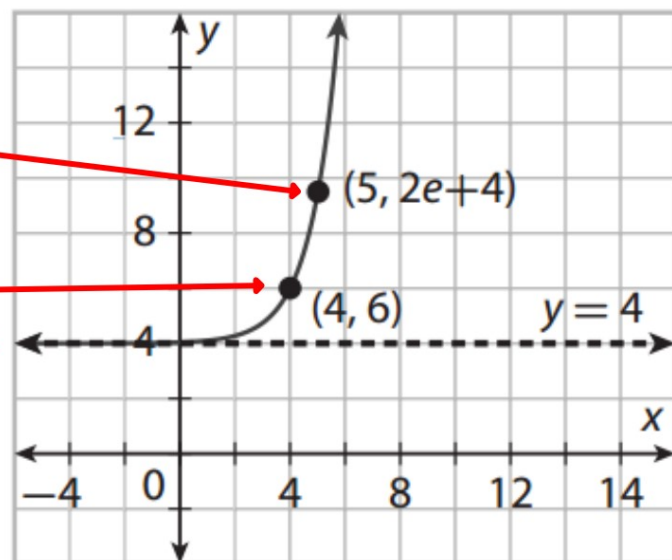
*second reference point*

$$(1 + h, ae + k)$$

$$(h, a + k)$$

*first reference point*

$$g(x) = 2e^{x-4} + 4$$



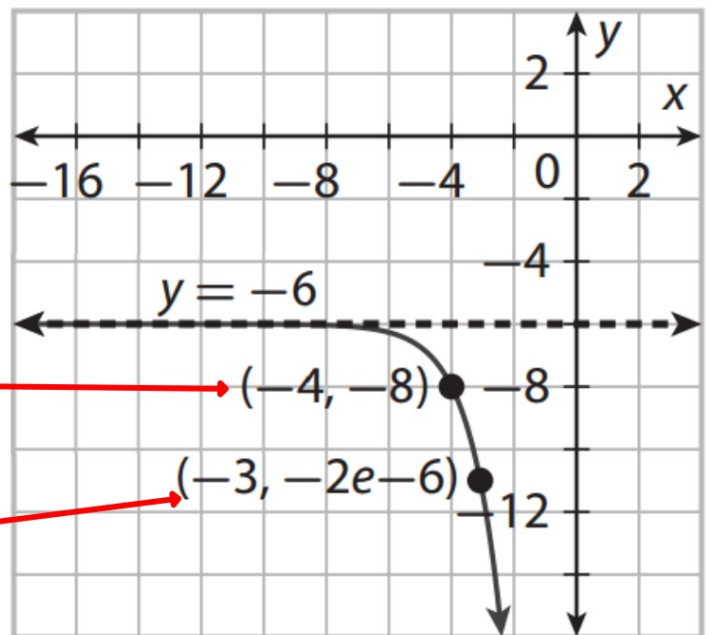
## The Base $e$

Writing Equations for Combined Transformations  
of  $f(x) = e^x$

$$g(x) = -2e^{x+4} - 6$$

$$g(x) = a \cdot e^{x-h} + k$$

*first point*  
 $(h, a + k)$   
 $(1 + h, ae + k)$   
*second point*



## The Base $e$

Take note

### Key Concept Continuously Compounded Interest

amount in account at time  $t$

interest rate (annual)

$$A(t) = P \cdot e^{rt}$$

Principal

time in years

**Scholarships** Suppose you won a contest at the start of 5th grade that deposited \$3000 in an account that pays 5% annual interest compounded continuously. How much will you have in the account when you enter high school 4 years later? Express the answer to the nearest dollar.



## The Base $e$

**Scholarships** Suppose you won a contest at the start of 5th grade that deposited \$3000 in an account that pays 5% annual interest compounded continuously. How much will you have in the account when you enter high school 4 years later? Express the answer to the nearest dollar.

$$A = P \cdot e^{rt} \quad \textit{Plug \& Chug!}$$

$$= 3000e^{(0.05)(4)} \quad \text{Substitute values for } P, r, \text{ and } t.$$

$$= 3000e^{0.2} \quad \text{Simplify.}$$

$$\approx 3664 \quad \text{Use a calculator. Round to the nearest dollar.}$$

The amount in the account, to the nearest dollar, is \$3664.  
Write your answer, 3664 in the grid.

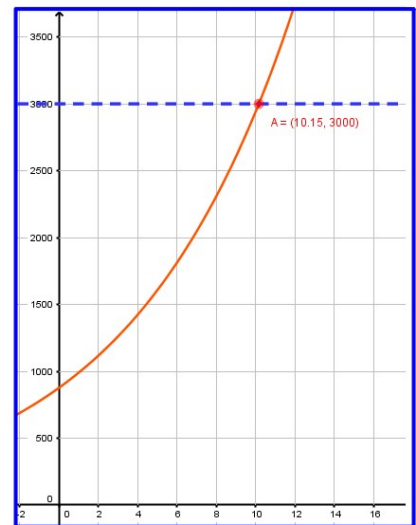
## The Base $e$

### Modeling with Exponential Functions Having Base $e$

The Dow Jones index is a stock market index for the New York Stock Exchange. The Dow Jones index for the period 1980-2000 can be modeled by  $V_{DJ}(t) = 878e^{0.121t}$ , where  $t$  is the number of years after 1980. Determine how many years after 1980 the Dow Jones index reached 3000.

$$3000 = 878(e^{0.121})^t$$

The value of the function is about 3000 when  $x \approx 10.2$ . So, the Dow Jones index reached 3000 after 10.2 years, or after the year 1990.

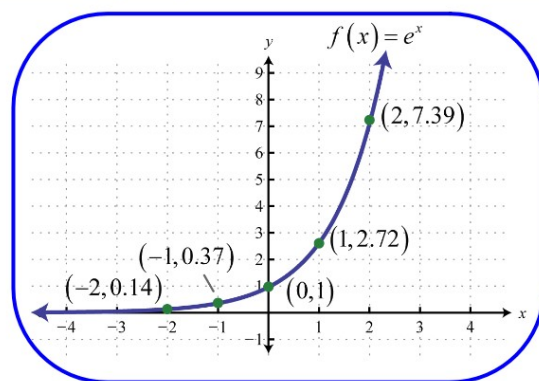


## **The Base $e$**

**Any Questions ?**

## The Base $e$

**Objectives** To explore the properties of functions of the form  $y = ab^x$   
To graph exponential functions that have base  $e$



**Classwork**

**Worksheet 13.3**

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